

$$\frac{d}{dt}(v) = a(t)$$

$$dv = a(t) \cdot dt$$

$$\int dv = \int a(t) \cdot dt$$

$$v = \int a(t) \cdot dt + A$$

$$v = b(t) + A \rightarrow (1)$$

where $b(t) = \int a(t) \cdot dt$ and A is constant of Integration

$$v = b(t) + A$$

$$(1) \Rightarrow \frac{dx}{dt} = b(t) + A$$

$$\Rightarrow \int dx = \int (b(t) + A) dt$$

$$\Rightarrow \int dx = \int b(t) dt + \int A dt$$

$$\Rightarrow x = \int b(t) \cdot dt + At + B \rightarrow (2)$$

where B is another constant of Integration.
The above method is used to solve a problem of time-dependent acc.

(iii) Velocity-dependent acc:

velocity-dependent acc depends on velocity only
i.e. $a = a(v)$. In such case we have

$$v \frac{dv}{dx} = a(v)$$

$$\Rightarrow dx = \frac{v dv}{a(v)}$$

$$\Rightarrow \int dx = \int \frac{v dv}{a(v)}$$

$$x = \int \frac{v}{a(v)} \cdot dv + C \rightarrow (1)$$

where C is constant of integration