

(15)

Angular velocity $\dot{\theta} = \frac{d\theta}{dt} = c$ (given)

Change in polar form put

$$x = r \cos \theta, \quad y = r \sin \theta \quad \text{in (1)}$$

$$x^2 \cos^2 \theta + y^2 \sin^2 \theta = a^2$$

$$r^2 = a^2 \Rightarrow r = a$$

$$\dot{r} = \frac{dr}{dt} = 0, \quad \ddot{r} = \frac{d^2r}{dt^2} = 0$$

As $\dot{\theta} = c$ and $\ddot{\theta} = 0$

As we know acceleration

$$\underline{a} = (\ddot{r} - r(\dot{\theta})^2) \hat{r} + (2\dot{r}\dot{\theta} + r\ddot{\theta}) \hat{s}$$

\therefore Radial Component of acceleration

$$a_r = 0 - a(c)^2$$

$$\boxed{a_r = -ac^2}$$

And transverse Component of acceleration

$$a_\theta = 2\dot{r}\dot{\theta} + r\ddot{\theta}$$

$$= 2(0)c + a \cdot 0 = 0$$

Q If the Components of velocity along and \perp to radius vector are λv^2 and μv^2 , then find the polar path of the Curve.

Sol:- As we know

$$v = \dot{r} \hat{r} + r\dot{\theta} \hat{s}$$

where radial Components of velocity

$$V_r = \dot{r} = \lambda v^2$$

And transverse Component of velocity

$$V_\theta = r\dot{\theta} = \mu v^2$$

$$\left(\dot{r} = \lambda v^2 \right)$$